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09/06/2013

Bharatiya Vidya Bhavan's  
**SARDAR PATEL COLLEGE OF ENGINEERING**

(An Autonomous Institution Affiliated to University of Mumbai)

m. E (c) with Sr.  
Sem I

JUNE 2013

Total Marks : 100

CLASS/SEM : ME Civil with  
Structural Engineering Subjects  
SEM I

Duration : 4 Hours

SUBJECT : STRUCTURAL DYNAMICS

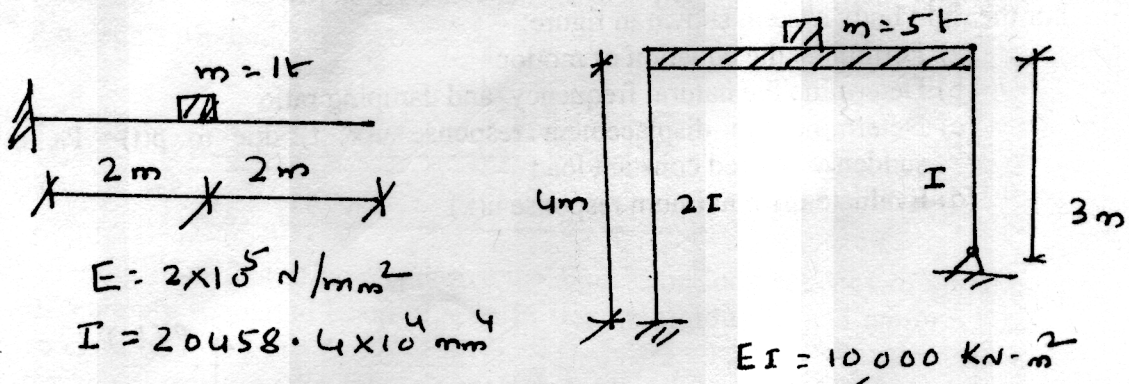
MASTER

- Attempt any FIVE questions out of SEVEN questions.
- Answers to all sub questions should be grouped together.
- Figures to the right indicate full marks.
- Assume suitable data if necessary and state the same clearly.

Q.1 a. Answer the following:

- Define Dynamic load. Distinguish between Prescribed and Random dynamic loads 3
- Explain clearly, the difference between static and dynamic analysis of structure 3

b. For the structural systems shown in figure compute the natural frequency of vibration 8



d. What is transmissibility of a system? Briefly explain how vibration isolation can be achieved 6.

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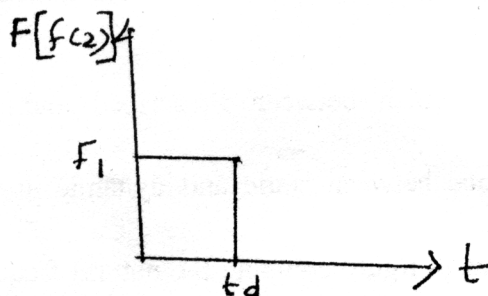
M.E.T.C) with Sr. Sem I 4/6/13

Q.2 a. The stiffness and damping properties of a mass spring system are to be determined by free vibration test. The mass is given as **200 kg**. In this, the mass is displaced by **10 mm** by a hydraulic jack and then suddenly released. At the end of **5 cycle**, the time is **1 seconds** and the amplitude is **4 mm**. Determine:

(i) Damped frequency (ii) Damping ratio (iii) Damping coefficient (iv) Undamped natural frequency (v) Stiffness coefficient

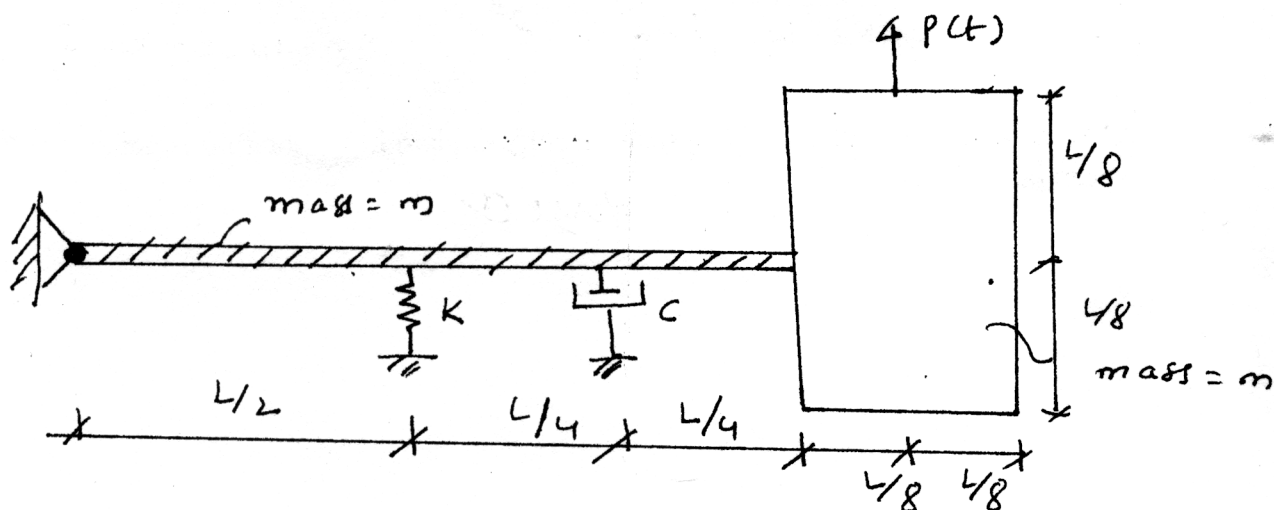
b. An SDOF system has a mass of 50 kg a damping ratio of 0.1, a natural frequency of 10 rad/sec and is subjected a harmonic excitation of amplitude 2500 N and frequency of 15 rad/sec. Determine the steady state amplitude.

c. For the pulse type force shown in figure, derive the expression for DLF



Q.3 For the rigid body system shown in figure:

- Formulate the equation of motion
- Determine the natural frequency and damping ratio
- Determine the displacement response  $u(x, t)$  due to  $p(t) = P_0$ , a suddenly applied constant load
- Evaluate the maximum response  $u(x)$



$$\begin{aligned}
 K &= 1000 \text{ kN/m} & m &= 100 \text{ kg} \\
 C &= 0.5 \text{ N-s/m} & L &= 4 \text{ m} \\
 P_0 &= 50 \text{ kN}
 \end{aligned}$$

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*m.e (ce) with m str. sem I str. Dynamics. 4/6/13.*

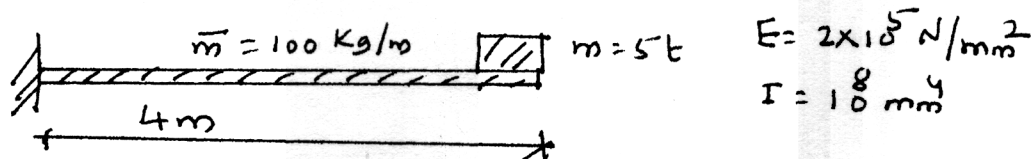
- Q.4 A three storey single bay frame has storey height of 4 m. each. All columns are 250 mm wide X 600 mm deep & beams are very stiff. The mass on each and floor is 30 t.  $E = 20000 \text{ Mpa}$ . Calculate natural frequencies & mode shapes 20

- Q.5 a. State and prove orthogonality principle. Also state the significance of orthogonality principle in dynamic analysis 5

- b. A three storey frame with free vibration characteristics as given below is subjected to a suddenly applied constant load of 100KN at 3<sup>rd</sup> floor level. Calculate maximum displacements of each storey. 15

Storey No.	Mass No.	Mass (t)	$\omega$ rad/sec	Mode shapes		
				$\Phi_{i1}$	$\Phi_{i2}$	$\Phi_{i3}$
1	1	20	15.73	0.399	0.747	1.0
2	2	20	49.85	1.0	0.727	-0.471
3	3	20	77.82	-0.908	1.0	-0.192

- Q.6 a. For the beam shown in figure calculate the fundamental frequency using Rayleigh's Method. 12



- b. Starting from first principle, derive the expression for frequency of vibration of a simply supported beam of span  $L$ , flexural rigidity  $EI$  and uniform mass  $m \text{ kg/m}$ . 8
- Q.7 a. Explain clearly how the dynamic analysis for Random dynamic load is done 5
- b. Explain the following in connection with random process 5
- (i) Random process (ii) Random variable (discrete and continuous)
  - (iii) Probability distributions (iv) Power spectral density functions (v) Auto correlation functions
- c. Derive the expression for steady state response of damped SDOF system subjected Sinusoidal force. 10

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